

# Application of IONOLAB-CIT to Central Europe for Regional Tomographic Reconstruction of Ionospheric Electron Density



HAKAN TUNA<sup>1</sup>, ORHAN ARIKAN<sup>1</sup>, FEZA ARIKAN<sup>2</sup>, UYGAR DEMİR<sup>2</sup>, CENK TOKER<sup>2</sup>, ZBYSEK MOSNA<sup>3</sup>, TAMARA L. GULYAEVA<sup>4</sup>

<sup>1</sup>Bilkent University, Department of Electrical and Electronics Engineering, Ankara, Turkey; <sup>2</sup>Hacettepe University, Department of Electrical and Electronics Engineering, Ankara, Turkey; <sup>3</sup>Institute of Atmospheric Physics, Academy of Sciences of the Czech Republic, Prague, Czech Republic; <sup>4</sup>IZMIRAN, Troitsk, Moscow Region, Russia

## INTRODUCTION

- Estimation of 3D electron density in the ionosphere is a crucial problem for investigating the ionospheric effects on electromagnetic propagation.
- Two important tools are generally used for investigating the ionosphere:

### ↓ GPS-TEC measurements

- widely used in ionospheric studies
- very sparse and non-uniform for employing 3D tomography methods (ill-conditioned problem)

### ↓ Ionospheric models like IRI-Plas

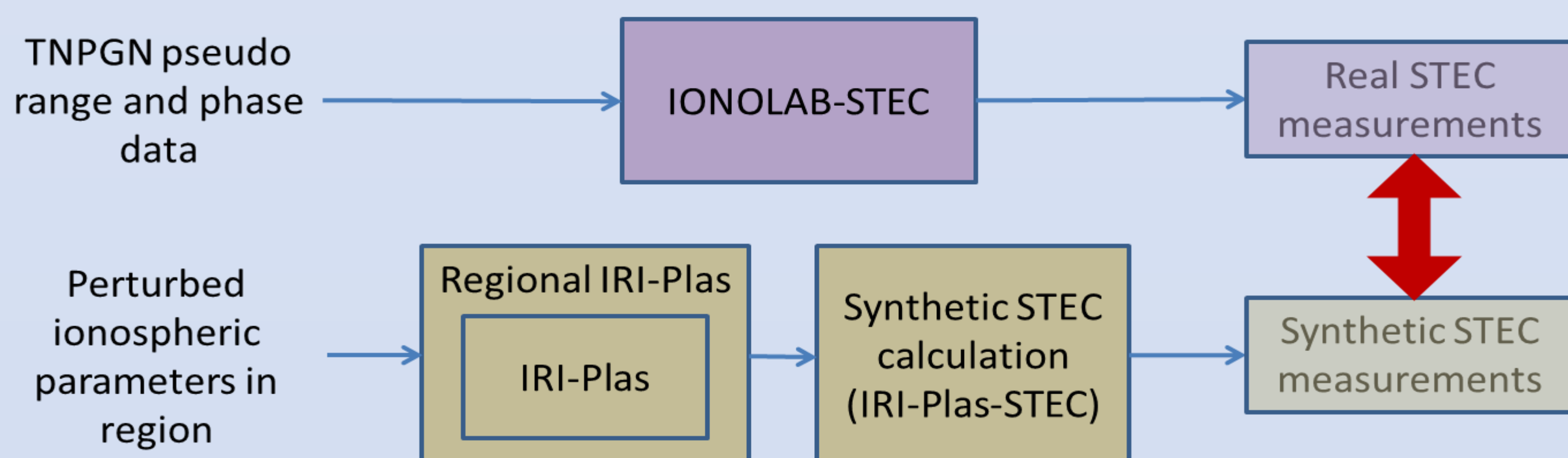
- can estimate monthly averages of 3D electron density distributions
- not generally compliant to the real measurements obtained from GPS receivers.

• In this study, a novel method for estimating the 3D electron density distribution in the ionosphere by using both GPS measurements over Central Europe.

• Proposed method **perturbs** default **ionospheric parameters** used in IRI-Plas model over a region of interest by using parametric perturbation surfaces, and **iteratively searches for the best physically feasible 3D electron density distribution**, which is compliant with the GPS-TEC measurements.

## PROBLEM DEFINITION

Find the optimum **perturbation values** on the selected ionospheric parameters in a region, such that, the resultant 3D electron density distribution generates synthetic STEC values similar to the real GPS-TEC measurements.



### Perturbation surfaces

$$f(\lambda, \phi) = m_1 \lambda' + m_2 \phi' + m_3$$

$$h(\lambda, \phi) = m_4 \lambda' + m_5 \phi' + m_6$$

$\lambda$  : latitude,  
 $\phi$  : longitude,

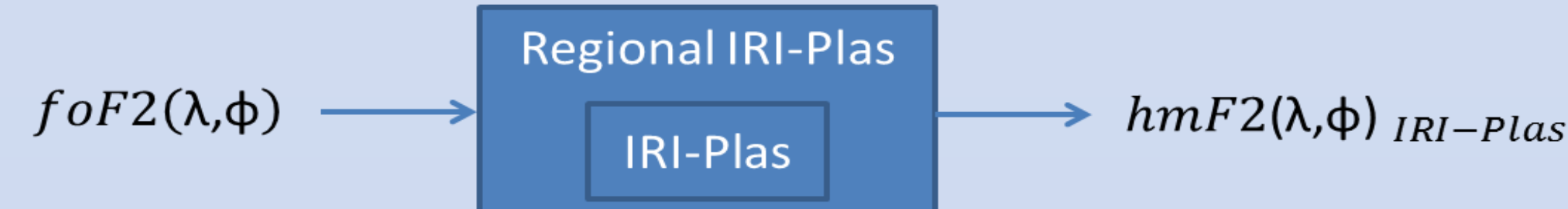
### Perturbed ionospheric parameters

$$foF2(\lambda, \phi) = foF2(\lambda, \phi)_{IRI-Plas} + f(\lambda, \phi)$$

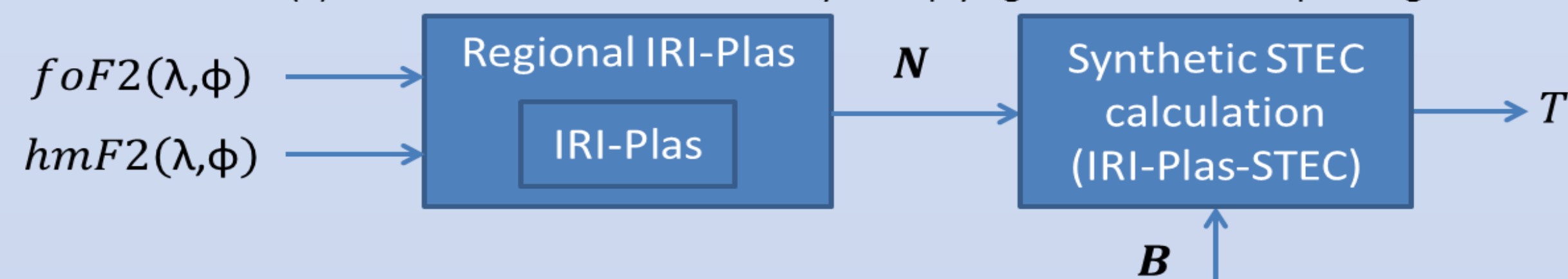
$$hmF2(\lambda, \phi) = hmF2(\lambda, \phi)_{IRI-Plas} + h(\lambda, \phi)$$

$\lambda'$  : normalized latitude [-1, 1]  
 $\phi'$  : normalized longitude [-1, 1]

Default IRI-Plas hmF2 values are obtained for given perturbed foF2



A synthetic 3D electron density distribution ( $N$ ) is computed from perturbed foF2 and hmF2 values, then any synthetic STEC value ( $T$ ) is calculated from this matrix by multiplying it with the corresponding  $B$  vector.



Objective: Minimize the following cost function

$$C = \frac{\|M - T\|}{\|M\|} + \rho \frac{\|H - H'\|^2}{\|H\|^2}$$

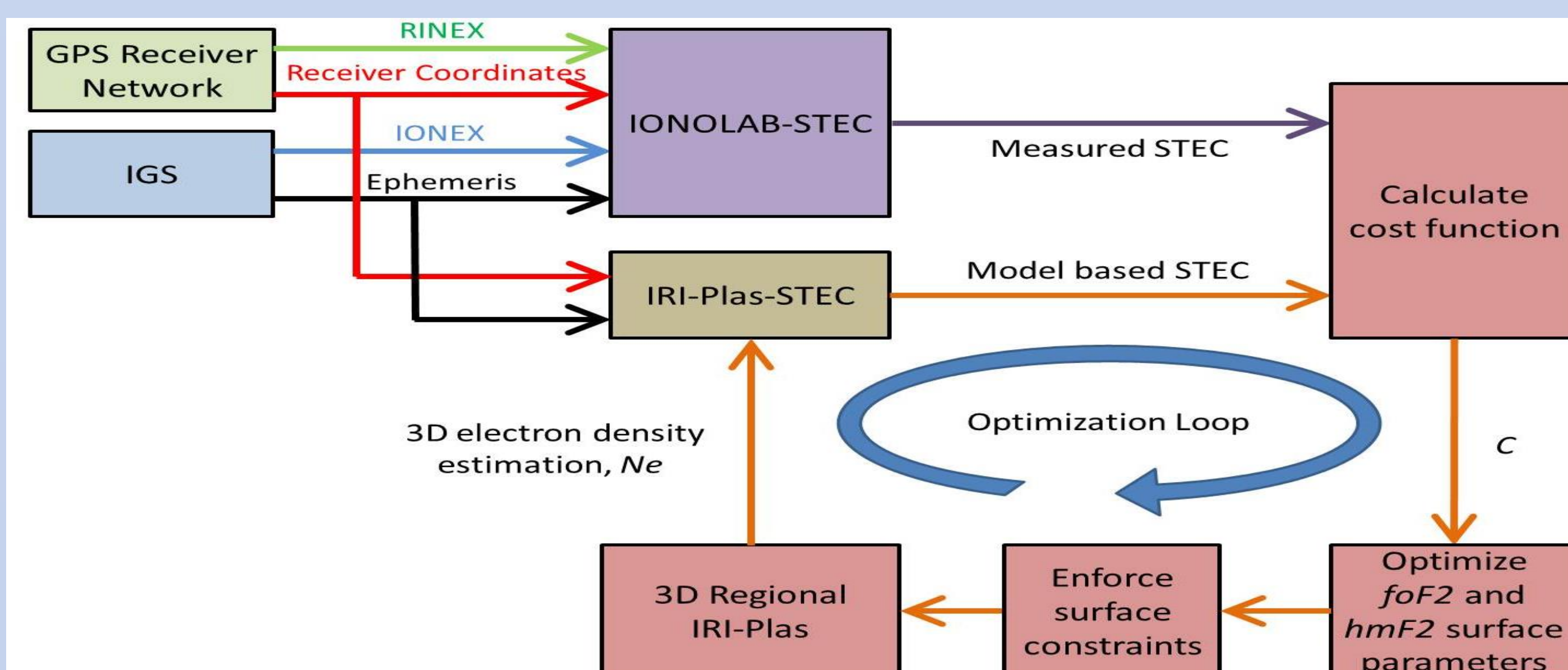
Deviation from physical relation between foF2 and hmF2 values

Relaxation parameter (used as 3 in simulations)

Difference between measured and calculated STEC values

- $M$ : The array containing measured GPS-TEC (IONOLAB-STEAC).
- $T$ : The array containing synthetic GPS-TEC (IRI-Plas-STEAC).
- $H$ : The array containing perturbed  $hmF2$  values.
- $H'$ : The array containing default  $hmF2$  values for given perturbed  $foF2$  values from IRI-Plas.

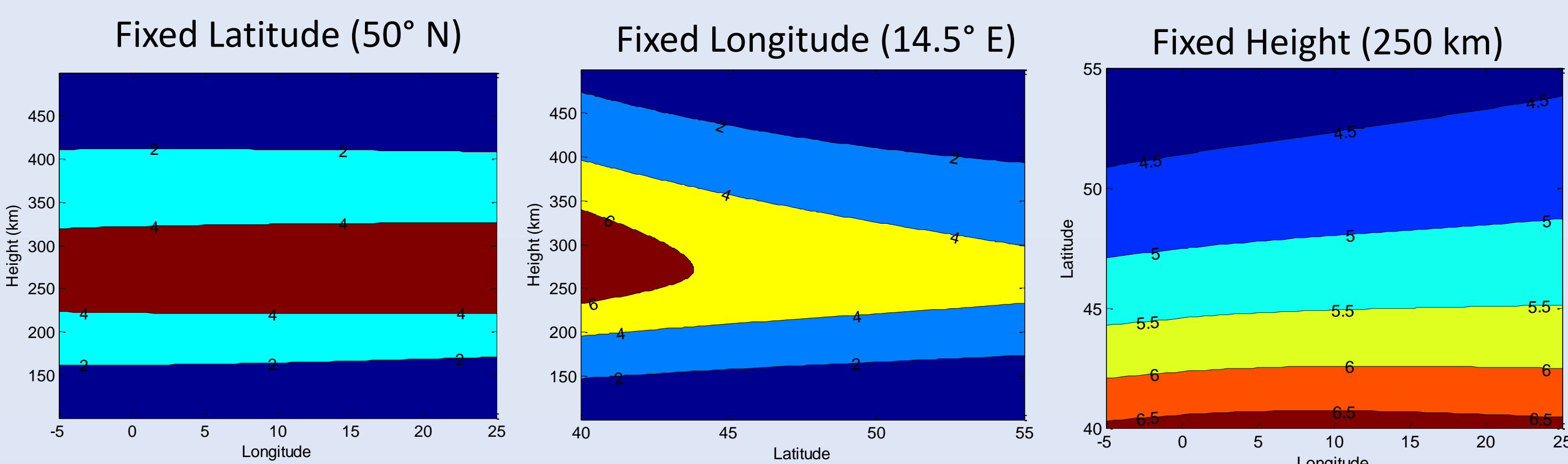
## IONOLAB-CIT



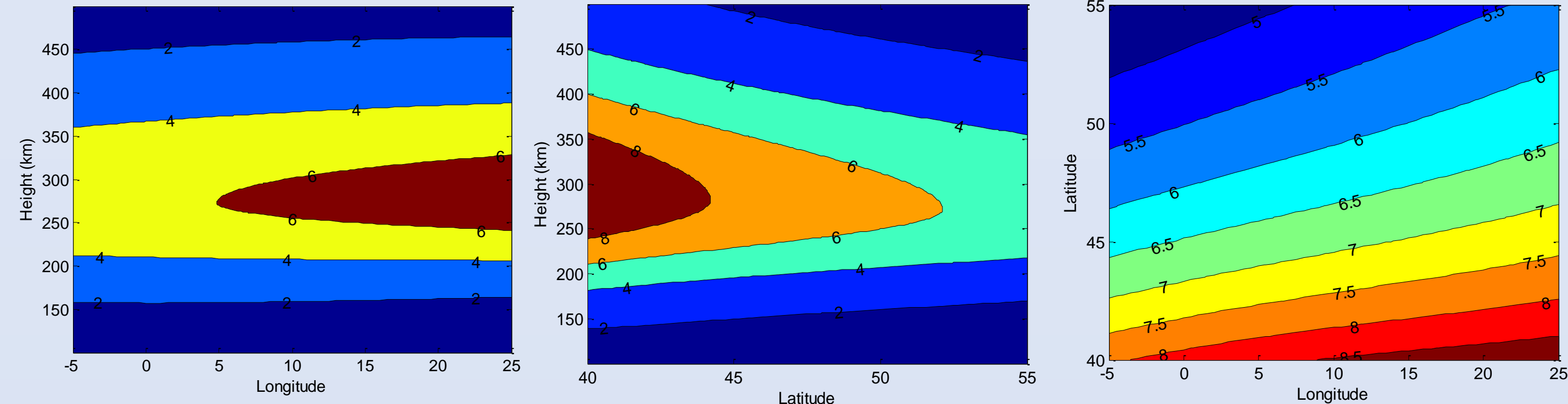
## RESULTS

(17 April 2011, 13:00 GMT, Calm)

IRI-Plas electron density slices ( $10^{11}$  el/m<sup>3</sup>)

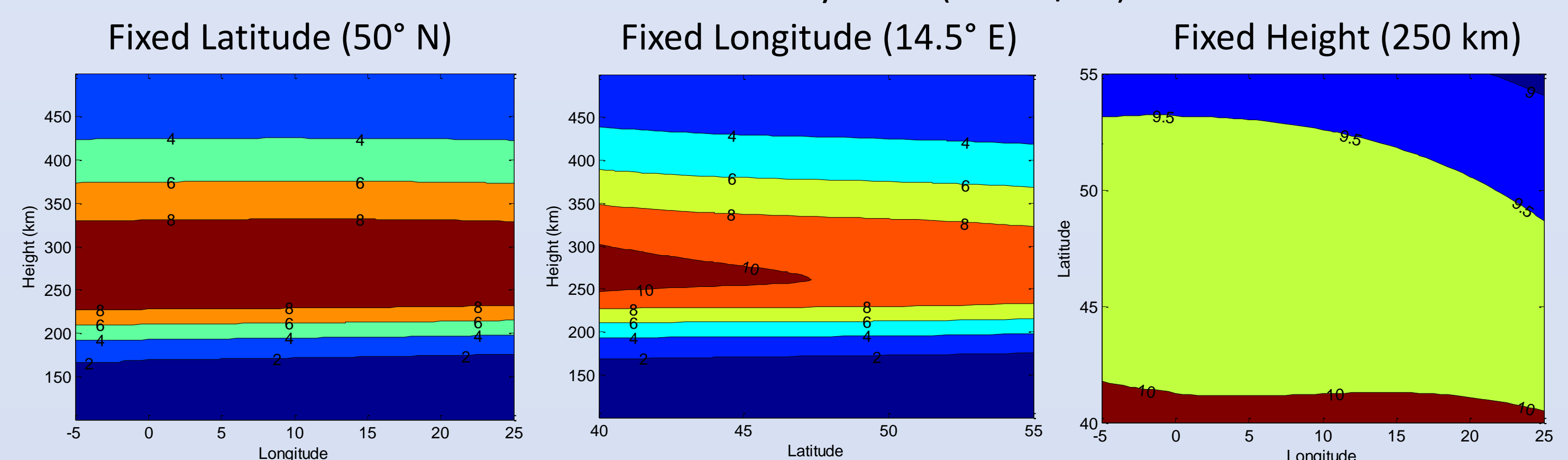


IONOLAB-CIT electron density slices ( $10^{11}$  el/m<sup>3</sup>)

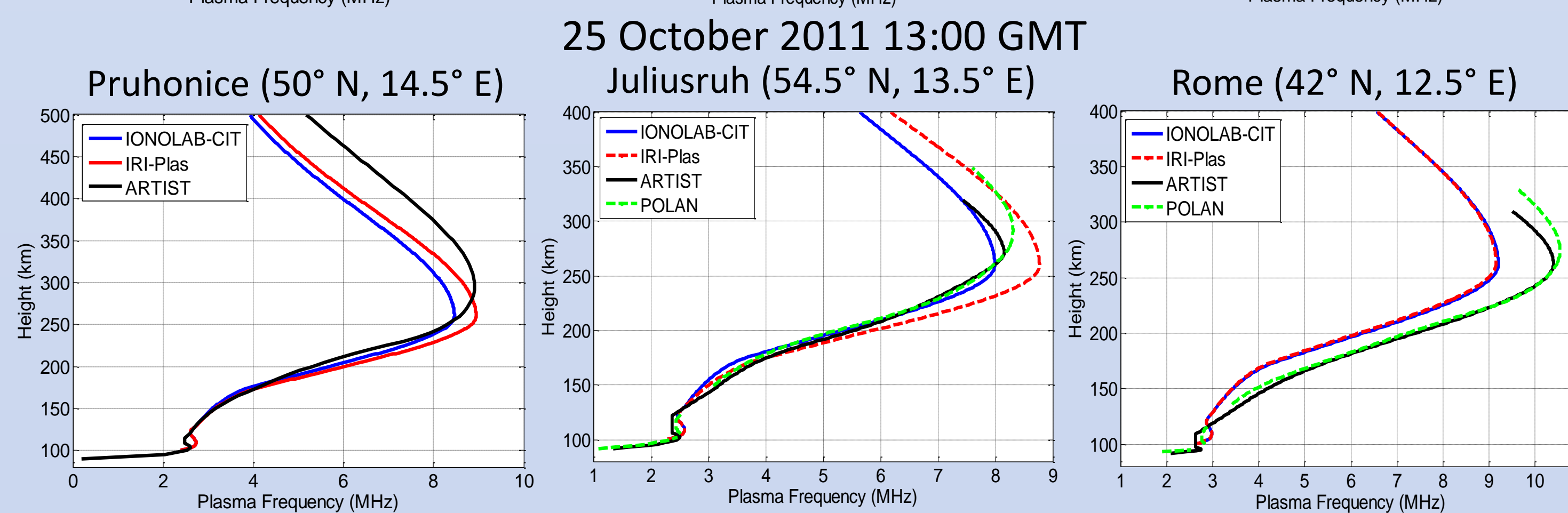
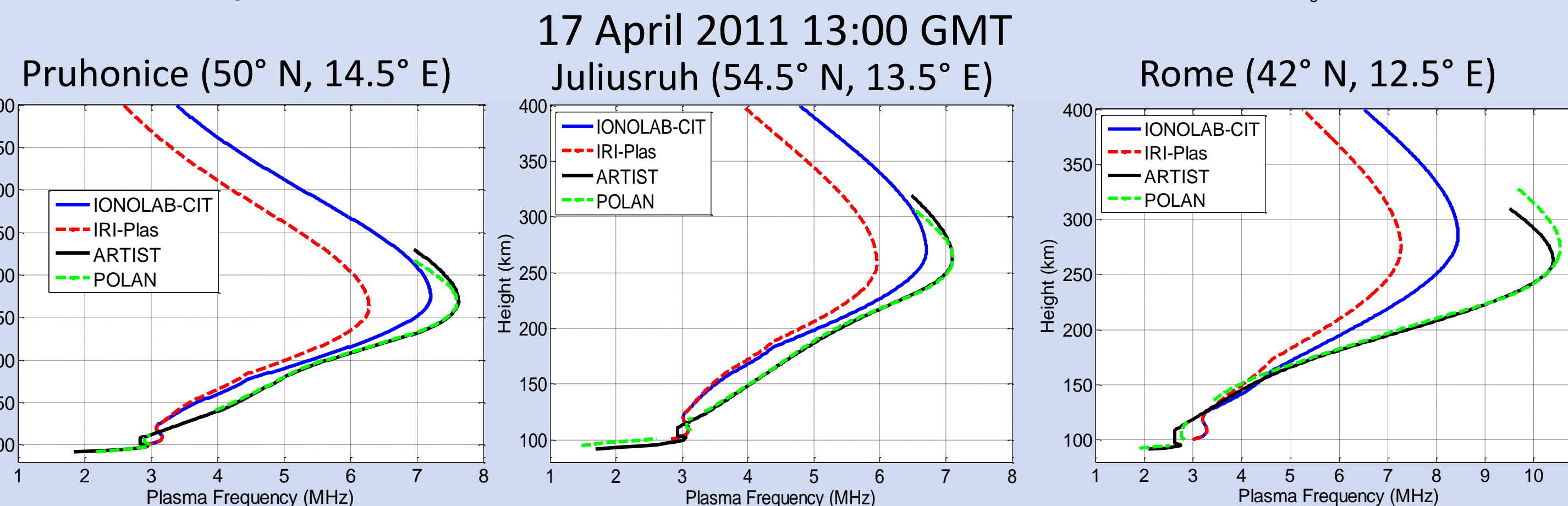
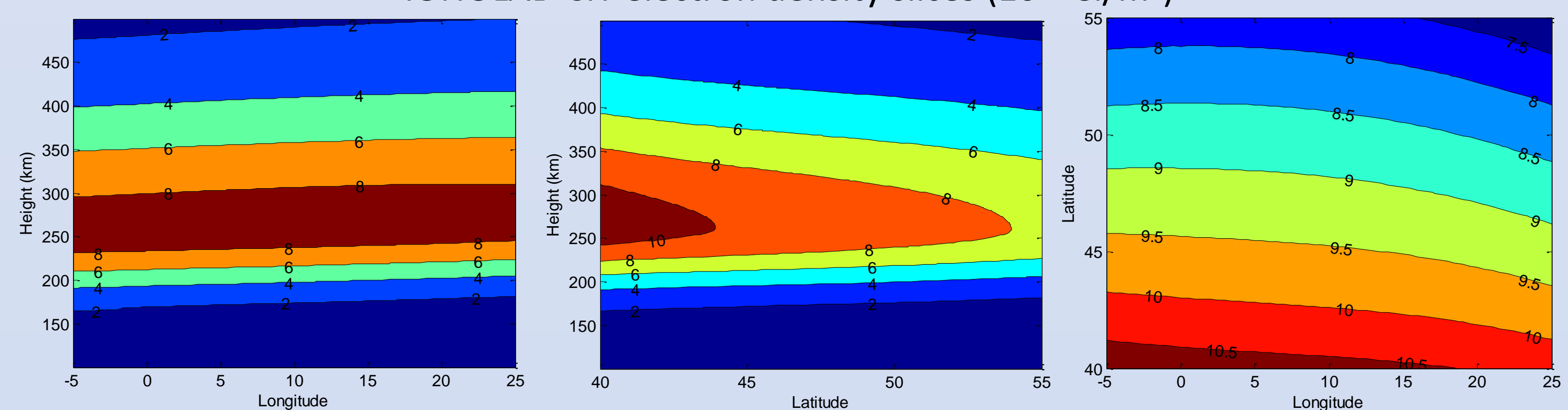


(25 October 2011, 13:00 GMT, Disturbed)

IRI-Plas electron density slices ( $10^{11}$  el/m<sup>3</sup>)



IONOLAB-CIT electron density slices ( $10^{11}$  el/m<sup>3</sup>)



## CONCLUSION

- Input parameters of IRI-Plas model are tuned in a way that the resulting 3D electron density profile is in compliance with GPS based STEC measurements and the input parameters are in compliance with each other.
- **foF2 and hmF2 values over Europe** are both represented with additive surface models with 3 parameters. The problem is reduced to a **6-parameter optimization** problem.
- **BFGS optimization method** is used for solving the optimization problem.
- Results show that the proposed methodology provides 3D electron density distributions compliant with both real GPS STEC measurements, and ionosonde measurements.
- Future works may consider temporal correlation of the optimization parameters which isn't involved in this study.

## Acknowledgement

This study is supported by TUBITAK 114E541, 115E915 and joint TUBITAK 114E092 and AS CR 14/001 projects. The GIM-TEC, Satellite DCB and ephemeris data that is used in computation of IONOLAB-STEAC is obtained from IGS Iono Working Group Data Analysis Center of Jet Propulsion Laboratory at <http://cdsis.gsfc.nasa.gov/pub/gps/products/ionex/>. TNPNG-Active RINEX data set is made available to IONOLAB group for TUBITAK 109E055 project. This data set can be accessed by the permission from TUBITAK and General Command of Mapping of Turkish Army (<http://www.hgk.msb.gov.tr/>). The Kp and Dst data are obtained from Data Analysis Center for Geomagnetism and Space Magnetism, Kyoto University, Japan ([http://wdc.kugi.kyoto-u.ac.jp/dst\\_realtime/index.html](http://wdc.kugi.kyoto-u.ac.jp/dst_realtime/index.html)) and <http://wdc.kugi.kyoto-u.ac.jp/kp/index.html>.

## REFERENCES

- [1] Arikan, F., C. B. Erol, and O. Arikan, Regularized estimation of vertical total electron content from Global Positioning System data, J. Geophys. Res., 108(A12), 2003.
- [2] Nayir, H., F. Arikan, O. Arikan, and C. B. Erol, Total Electron Content estimation with Reg-Est, J. Geophys. Res., 112, 2007.
- [3] Arikan, F., H. Nayir, U. Sezen, and O. Arikan, Estimation of single station interferometry receiver bias using GPS-TEC, Radio Sci., 43, 2008.
- [4] Tuna, H. Tuna, O. Arikan, F. Arikan, T. Gulyaeva, U. Sezen, "Online user-friendly slant total electron content computation from IRI-Plas: IRI-Plas-STEAC", Space Weather, 12, 2014
- [5] Hakan Tuna, Orhan Arikan, F. Arikan, "Regional model-based computerized ionospheric tomography using GPS measurements: IONOLAB-CIT", Radio Science, 50, 1062-1075, 2015

